



# Formal Verification of Cryptographic Protocols in Spi-Calculus

Eijiro Sumii

Tohoku University

# Caution

- ◆ Literature on spi-calculus is confusing
  - Inconsistent terminology
  - Some "results" found too weak or even wrong
- ◆ This talk is my own combination of various results on spi-calculus





# Outline

- ◆ What is spi-calculus?
  - Syntax and operational semantics
- ◆ Example protocol
- ◆ Attack against the example protocol
- ◆ Formalizing secrecy by non-interference
- ◆ Proving secrecy by hedged bisimulations
- ◆ Conclusions



# What is spi-calculus?

## [Abadi-Gordon 99]

- ◆ spi-calculus =  $\pi$ -calculus + (shared-key) perfect encryption primitives

The only equation is:

$$\text{dec}(\text{enc}(\text{Msg}, \text{key}), \text{key}) = \text{Msg}$$

Cf. Textbook RSA is malleable:

$$\begin{aligned} \text{enc}(\text{Msg}_1, \text{pubkey}) \times \text{enc}(\text{Msg}_2, \text{pubkey}) \\ = \text{enc}(\text{Msg}_1 \times \text{Msg}_2, \text{pubkey}) \end{aligned}$$

# Syntax

$M, N ::=$	message
$x$	name
$\{M_1, \dots, M_n\}_N$	ciphertext
$P, Q, R ::=$	process
$0$	inaction
$\overline{M}\langle N \rangle.P$	sending
$M(x).P$	receiving
$P \mid Q$	parallel composition
$(\nu x)P$	restriction
$!P$	replication
$\text{case } M \text{ of } \{x_1, \dots, x_n\}_N \text{ in } P$	decryption
$[M = N]P$	matching

# Operational Semantics (1/2): Structural Equivalence

case  $\{M_1, \dots, M_n\}_N$  of  $\{x_1, \dots, x_n\}_N$  in  $P$   
 $\equiv [M_1, \dots, M_n/x_1, \dots, x_n]P$

$$[M = M]P \equiv P \quad !P \equiv P \mid !P$$

$$P \mid (\nu x)Q \equiv (\nu x)(P \mid Q) \quad \text{if } x \notin \text{free}(P)$$

$$P \mid 0 \equiv P \quad P \mid Q \equiv Q \mid P \quad (P \mid Q) \mid R \equiv P \mid (Q \mid R)$$

$$\frac{P \equiv P'}{P \mid Q \equiv P' \mid Q}$$

$$\frac{P \equiv P'}{(\nu x)P \equiv (\nu x)P'}$$

$$P \equiv P \quad \frac{P \equiv Q}{Q \equiv P} \quad \frac{P \equiv Q \quad Q \equiv R}{P \equiv R}$$

# Operational Semantics (2/2): Reaction Relation

$$\bar{x}\langle M \rangle.P \mid x(y).Q \rightarrow P \mid [M/y]Q$$

$$\frac{P \equiv P' \quad P' \rightarrow Q' \quad Q' \equiv Q}{P \rightarrow Q}$$

$$\frac{P \rightarrow P'}{P \mid Q \rightarrow P' \mid Q}$$

$$\frac{P \rightarrow P'}{(\nu x)P \rightarrow (\nu x)P'}$$



# Outline

- ◆ What is spi-calculus?
  - Syntax and operational semantics
- ◆ Example protocol
- ◆ Attack against the example protocol
- ◆ Formalizing secrecy by non-interference
- ◆ Proving secrecy by hedged bisimulations
- ◆ Conclusions



# Example: A Naive Protocol (Wide Mouthed Frog Protocol)

1.  $A \rightarrow S : \{K_{AB}\}_{K_{AS}}$
2.  $S \rightarrow B : \{K_{AB}\}_{K_{BS}}$
3.  $B \rightarrow A : \{M\}_{K_{AB}}$

$$P_A = (\nu K_{AB}) \overline{c_{AS}} \langle \{K_{AB}\}_{K_{AS}} \rangle.$$

$$c_{AB}(n). \text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0$$

$$P_S = c_{AS}(x). \text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c_{BS}} \langle \{y\}_{K_{BS}} \rangle$$

$$P_B = c_{BS}(x). \text{case } x \text{ of } \{y\}_{K_{BS}} \text{ in } \overline{c_{AB}} \langle \{M\}_y \rangle$$

The whole system is:

$$(\nu K_{AS})(\nu K_{BS})(P_A \mid P_S \mid P_B)$$

# How does the protocol run? (1/2)

$$\begin{aligned}
 & (\nu K_{AS})(\nu K_{BS})(P_A \mid P_S \mid P_B) \\
 \equiv & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB}) \\
 & \quad (\overline{c_{AS}}\langle\{K_{AB}\}_{K_{AS}}\rangle.c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid \\
 & \quad \quad c_{AS}(x).\text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c_{BS}}\langle\{y\}_{K_{BS}}\rangle \mid \\
 & \quad \quad c_{BS}(x).\text{case } x \text{ of } \{y\}_{K_{BS}} \text{ in } \overline{c_{AB}}\langle\{M\}_y\rangle) \\
 \rightarrow & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB}) \\
 & \quad (\overline{c_{AB}}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid \\
 & \quad \quad \text{case } \{K_{AB}\}_{K_{AS}} \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c_{BS}}\langle\{y\}_{K_{BS}}\rangle \mid \\
 & \quad \quad c_{BS}(x).\text{case } x \text{ of } \{y\}_{K_{BS}} \text{ in } \overline{c_{AB}}\langle\{M\}_y\rangle) \\
 \equiv & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB}) \\
 & \quad (\overline{c_{AB}}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid \\
 & \quad \quad \overline{c_{BS}}\langle\{K_{AB}\}_{K_{BS}}\rangle \mid \\
 & \quad \quad c_{BS}(x).\text{case } x \text{ of } \{y\}_{K_{BS}} \text{ in } \overline{c_{AB}}\langle\{M\}_y\rangle)
 \end{aligned}$$

# How does the protocol run? (2/2)



$$\begin{aligned}
 & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB}) \\
 & \quad (c_{AB}(n). \text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid \\
 & \quad \quad \overline{c_{BS}}\langle\{K_{AB}\}_{K_{BS}}\rangle \mid \\
 & \quad \quad c_{BS}(x). \text{case } x \text{ of } \{y\}_{K_{BS}} \text{ in } \overline{c_{AB}}\langle\{M\}_y\rangle) \\
 \rightarrow & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB}) \\
 & \quad (c_{AB}(n). \text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid \\
 & \quad \quad \text{case } \{K_{AB}\}_{K_{BS}} \text{ of } \{y\}_{K_{BS}} \text{ in } \overline{c_{AB}}\langle\{M\}_y\rangle) \\
 \equiv & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB}) \\
 & \quad (c_{AB}(n). \text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid \\
 & \quad \quad \overline{c_{AB}}\langle\{M\}_{K_{AB}}\rangle) \\
 \rightarrow & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB}) \\
 & \quad \text{case } \{M\}_{K_{AB}} \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \\
 \equiv & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB})0
 \end{aligned}$$

# How does the protocol run? (2/2)




$$\begin{aligned}
 & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB}) \\
 & \quad (c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid \\
 & \quad \quad \overline{c_{BS}}\langle\{K_{AB}\}_{K_{BS}}\rangle \mid \\
 & \quad \quad c_{BS}(x).\text{case } x \text{ of } \{y\}_{K_{BS}} \text{ in } \overline{c_{AB}}\langle\{M\}_y\rangle) \\
 \rightarrow & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB}) \\
 & \quad (c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid \\
 & \quad \quad \text{case } \{K_{AB}\}_{K_{BS}} \text{ of } \{y\}_{K_{BS}} \text{ in } \overline{c_{AB}}\langle\{M\}_y\rangle) \\
 \equiv & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB}) \\
 & \quad (\overline{c_{AB}}\langle\{M\}_{K_{AB}}\rangle) \\
 \rightarrow & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB}) \\
 & \quad \text{case } \{M\}_{K_{AB}} \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \\
 \equiv & (\nu K_{AS})(\nu K_{BS})(\nu K_{AB})0
 \end{aligned}$$



# Outline

- ◆ What is spi-calculus?
  - Syntax and operational semantics
- ◆ Example protocol
- ◆ Attack against the example protocol
- ◆ Formalizing secrecy by non-interference
- ◆ Proving secrecy by hedged bisimulations
- ◆ Conclusions

# Parallel runs of the protocol (1/2)

- 
1.  $A \rightarrow S : \{K_{AB}\}_{K_{AS}}$
  2.  $S \rightarrow B : \{K_{AB}\}_{K_{BS}}$
  3.  $B \rightarrow A : \{M\}_{K_{AB}}$
  
  - 1'.  $B \rightarrow S : \{K_{BE}\}_{K_{BS}}$
  - 2'.  $S \rightarrow E : \{K_{BE}\}_{K_{ES}}$
  - 3'.  $E \rightarrow B : \{M'\}_{K_{BE}}$

# Parallel runs of the protocol (2/2)

$$P_A = (\nu K_{AB}) \overline{c_{AS}} \langle \{K_{AB}\}_{K_{AS}} \rangle.$$

$$c_{AB}(n). \text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0$$

$$P_S = c_{AS}(x). \text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c_{BS}} \langle \{y\}_{K_{BS}} \rangle$$

$$| c'_{BS}(x'). \text{case } x' \text{ of } \{y'\}_{K_{BS}} \text{ in } \overline{c_{ES}} \langle \{y'\}_{K_{ES}} \rangle$$

$$P_B = c_{BS}(x). \text{case } x \text{ of } \{y\}_{K_{BS}} \text{ in } \overline{c_{AB}} \langle \{M\}_y \rangle$$

$$| (\nu K_{BE}) \overline{c'_{BS}} \langle \{K_{BE}\}_{K_{BS}} \rangle.$$

$$c_{BE}(n'). \text{case } n' \text{ of } \{m'\}_{K_{BE}} \text{ in } 0$$

$$P_E = c_{ES}(x'). \text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in } \overline{c_{BE}} \langle \{M'\}_{y'} \rangle$$



## Exercise (?)

- ◆ Write down the reduction of  $(\forall K_{AS})(\forall K_{BS})(\forall K_{ES})(P_A \mid P_S \mid P_B \mid P_E)$ .





## What if E is evil in fact?

- ◆ Assumption: attacker has full access to open channels (Dolev-Yao model)
- ◆ Result: not only  $M'$  but also  $M$  may leak!

$$1'_a. B \rightarrow E(S) : \{K_{BE}\}_{K_{BS}}$$

$$2. E(S) \rightarrow B : \{K_{BE}\}_{K_{BS}}$$

$$1'_b. E(B) \rightarrow S : \{K_{BE}\}_{K_{BS}}$$

$$2'. S \rightarrow E : \{K_{BE}\}_{K_{ES}}$$

$$3. B \rightarrow E(A) : \{M\}_{K_{BE}}$$

# How does the attack work?

$$P'_E = c'_{BS}(z).\overline{c_{BS}}\langle z\rangle.c'_{BS}\langle z\rangle.$$

$$c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in}$$

$$c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m$$

$$\equiv P'_E \mid (\nu K_{AS})(\nu K_{BS})(P_A \mid P_S \mid P_B)$$

$$\equiv (\nu K_{AS})(\nu K_{BS})(\nu K_{AB})(\nu K_{BE})$$

$$(c'_{BS}(z).\overline{c_{BS}}\langle z\rangle.c'_{BS}\langle z\rangle.$$

$$c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in}$$

$$c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m \mid$$

$$\overline{c_{AS}}\langle \{K_{AB}\}_{K_{AS}} \rangle.c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid$$

$$c_{AS}(x).\text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c_{BS}}\langle \{y\}_{K_{BS}} \rangle \mid$$

$$c'_{BS}(x').\text{case } x' \text{ of } \{y'\}_{K_{BS}} \text{ in } \overline{c_{ES}}\langle \{y'\}_{K_{ES}} \rangle \mid$$

$$c_{BS}(x).\text{case } x \text{ of } \{y\}_{K_{BS}} \text{ in } \overline{c_{AB}}\langle \{M\}_y \rangle \mid$$

$$\overline{c'_{BS}}\langle \{K_{BE}\}_{K_{BS}} \rangle.c_{BE}(n').\text{case } n' \text{ of } \{m'\}_{K_{BE}} \text{ in } 0)$$

# How does the attack work?

$$P'_E = c'_{BS}(z).\overline{c}_{BS}\langle z\rangle.c'_{BS}\langle z\rangle.$$

$$c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in}$$

$$c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m$$

$$\rightarrow P'_E \mid (\nu K_{AS})(\nu K_{BS})(P_A \mid P_S \mid P_B)$$

$$(\nu K_{AS})(\nu K_{BS})(\nu K_{AB})(\nu K_{BE})$$

$$(\overline{c}_{BS}\langle \{K_{BE}\}_{K_{BS}} \rangle.c'_{BS}\langle \{K_{BE}\}_{K_{BS}} \rangle.$$

$$c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in}$$

$$c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m \mid$$

$$\overline{c}_{AS}\langle \{K_{AB}\}_{K_{AS}} \rangle.c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid$$

$$c_{AS}(x).\text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c}_{BS}\langle \{y\}_{K_{BS}} \rangle \mid$$

$$c'_{BS}(x').\text{case } x' \text{ of } \{y'\}_{K_{BS}} \text{ in } \overline{c}_{ES}\langle \{y'\}_{K_{ES}} \rangle \mid$$

$$c_{BS}(x).\text{case } x \text{ of } \{y\}_{K_{BS}} \text{ in } \overline{c}_{AB}\langle \{M\}_{y'} \rangle \mid$$

$$c_{BE}(n').\text{case } n' \text{ of } \{m'\}_{K_{BE}} \text{ in } 0)$$

# How does the attack work?

$$P'_E = c'_{BS}(z).\overline{c}_{BS}\langle z\rangle.c'_{BS}\langle z\rangle.$$

$$c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in}$$

$$c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m$$

$$\rightarrow P'_E \mid (\nu K_{AS})(\nu K_{BS})(P_A \mid P_S \mid P_B)$$

$$(\nu K_{AS})(\nu K_{BS})(\nu K_{AB})(\nu K_{BE})$$

$$(\overline{c}_{BS}\langle \{K_{BE}\}_{K_{BS}} \rangle.c'_{BS}\langle \{K_{BE}\}_{K_{BS}} \rangle.$$

$$c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in}$$

$$c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m \mid$$

$$\overline{c}_{AS}\langle \{K_{AB}\}_{K_{AS}} \rangle.c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid$$

$$c_{AS}(x).\text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c}_{BS}\langle \{y\}_{K_{BS}} \rangle \mid$$

$$c'_{BS}(x').\text{case } x' \text{ of } \{y'\}_{K_{BS}} \text{ in } \overline{c}_{ES}\langle \{y'\}_{K_{ES}} \rangle \mid$$

$$c_{BS}(x).\text{case } x \text{ of } \{y\}_{K_{BS}} \text{ in } \overline{c}_{AB}\langle \{M\}_{y'} \rangle \mid$$

$$c_{BE}(n').\text{case } n' \text{ of } \{m'\}_{K_{BE}} \text{ in } 0)$$

# How does the attack work?

$$P'_E = c'_{BS}(z).\overline{c}_{BS}\langle z\rangle.c'_{BS}\langle z\rangle.$$

$$c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in}$$

$$c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m$$

$$\rightarrow^* P'_E \mid (\nu K_{AS})(\nu K_{BS})(P_A \mid P_S \mid P_B)$$

$$(\nu K_{AS})(\nu K_{BS})(\nu K_{AB})(\nu K_{BE})$$

$$(c'_{BS}\langle \{K_{BE}\}_{K_{BS}} \rangle.$$

$$c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in}$$

$$c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m \mid$$

$$\overline{c}_{AS}\langle \{K_{AB}\}_{K_{AS}} \rangle.c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid$$

$$c_{AS}(x).\text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c}_{BS}\langle \{y\}_{K_{BS}} \rangle \mid$$

$$c'_{BS}(x').\text{case } x' \text{ of } \{y'\}_{K_{BS}} \text{ in } \overline{c}_{ES}\langle \{y'\}_{K_{ES}} \rangle \mid$$

$$\overline{c}_{AB}\langle \{M\}_{K_{BE}} \rangle \mid$$

$$c_{BE}(n').\text{case } n' \text{ of } \{m'\}_{K_{BE}} \text{ in } 0)$$

# How does the attack work?

$$P'_E = c'_{BS}(z).\overline{c}_{BS}\langle z\rangle.c'_{BS}\langle z\rangle.$$

$$c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in}$$

$$c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m$$

$$\rightarrow^* P'_E \mid (\nu K_{AS})(\nu K_{BS})(P_A \mid P_S \mid P_B)$$

$$(\nu K_{AS})(\nu K_{BS})(\nu K_{AB})(\nu K_{BE})$$

$$(c'_{BS}\langle \{K_{BE}\}_{K_{BS}} \rangle.$$

$$c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in}$$

$$c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m \mid$$

$$\overline{c}_{AS}\langle \{K_{AB}\}_{K_{AS}} \rangle.c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid$$

$$c_{AS}(x).\text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c}_{BS}\langle \{y\}_{K_{BS}} \rangle \mid$$

$$c'_{BS}(x').\text{case } x' \text{ of } \{y'\}_{K_{BS}} \text{ in } \overline{c}_{ES}\langle \{y'\}_{K_{ES}} \rangle \mid$$

$$\overline{c}_{AB}\langle \{M\}_{K_{BE}} \rangle \mid$$

$$c_{BE}(n').\text{case } n' \text{ of } \{m'\}_{K_{BE}} \text{ in } 0)$$

# How does the attack work?

$$P'_E = c'_{BS}(z).\overline{c_{BS}}\langle z\rangle.c'_{BS}\langle z\rangle.$$

$$c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in}$$

$$c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m$$

$$\rightarrow^* P'_E \mid (\nu K_{AS})(\nu K_{BS})(P_A \mid P_S \mid P_B)$$

$$(\nu K_{AS})(\nu K_{BS})(\nu K_{AB})(\nu K_{BE})$$

$$\left( c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in} \right.$$

$$\left. c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m \mid \right.$$

$$\left. \overline{c_{AS}}\langle \{K_{AB}\}_{K_{AS}} \rangle.c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid \right.$$

$$\left. c_{AS}(x).\text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c_{BS}}\langle \{y\}_{K_{BS}} \rangle \mid \right.$$

$$\left. \overline{c_{ES}}\langle \{K_{BE}\}_{K_{ES}} \rangle \mid \right.$$

$$\left. \overline{c_{AB}}\langle \{M\}_{K_{BE}} \rangle \mid \right.$$

$$c_{BE}(n').\text{case } n' \text{ of } \{m'\}_{K_{BE}} \text{ in } 0)$$

# How does the attack work?

$$P'_E = c'_{BS}(z).\overline{c}_{BS}\langle z\rangle.c'_{BS}\langle z\rangle. \\ c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in} \\ c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m$$

$$\rightarrow^* P'_E \mid (\nu K_{AS})(\nu K_{BS})(P_A \mid P_S \mid P_B) \\ (\nu K_{AS})(\nu K_{BS})(\nu K_{AB})(\nu K_{BE}) \\ (c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{BE}} \text{ in DoEvil}_m \mid \\ \overline{c}_{AS}\langle \{K_{AB}\}_{K_{AS}} \rangle.c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid \\ c_{AS}(x).\text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c}_{BS}\langle \{y\}_{K_{BS}} \rangle \mid \\ \overline{c}_{AB}\langle \{M\}_{K_{BE}} \rangle \mid \\ c_{BE}(n').\text{case } n' \text{ of } \{m'\}_{K_{BE}} \text{ in } 0)$$



# How does the attack work?

$$P'_E = c'_{BS}(z).\overline{c}_{BS}\langle z\rangle.c'_{BS}\langle z\rangle. \\ c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in} \\ c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m$$

$$\rightarrow^* P'_E \mid (\nu K_{AS})(\nu K_{BS})(P_A \mid P_S \mid P_B) \\ (\nu K_{AS})(\nu K_{BS})(\nu K_{AB})(\nu K_{BE}) \\ (c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{BE}} \text{ in DoEvil}_m \mid \\ \overline{c}_{AS}\langle \{K_{AB}\}_{K_{AS}} \rangle.c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid \\ c_{AS}(x).\text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c}_{BS}\langle \{y\}_{K_{BS}} \rangle \mid \\ \overline{c}_{AB}\langle \{M\}_{K_{BE}} \rangle \mid \\ c_{BE}(n').\text{case } n' \text{ of } \{m'\}_{K_{BE}} \text{ in } 0)$$

# How does the attack work?

$$P'_E = c'_{BS}(z).\overline{c}_{BS}\langle z\rangle.c'_{BS}\langle z\rangle. \\ c_{ES}(x').\text{case } x' \text{ of } \{y'\}_{K_{ES}} \text{ in} \\ c_{AB}(n).\text{case } n \text{ of } \{m\}_{y'} \text{ in DoEvil}_m$$

$$\rightarrow^* P'_E \mid (\nu K_{AS})(\nu K_{BS})(P_A \mid P_S \mid P_B) \\ (\nu K_{AS})(\nu K_{BS})(\nu K_{AB})(\nu K_{BE}) \\ (\text{DoEvil}_M \mid \\ \overline{c}_{AS}\langle \{K_{AB}\}_{K_{AS}} \rangle.c_{AB}(n).\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \mid \\ c_{AS}(x).\text{case } x \text{ of } \{y\}_{K_{AS}} \text{ in } \overline{c}_{BS}\langle \{y\}_{K_{BS}} \rangle \mid \\ c_{BE}(n').\text{case } n' \text{ of } \{m'\}_{K_{BE}} \text{ in } 0)$$



# Outline

- ◆ What is spi-calculus?
  - Syntax and operational semantics
- ◆ Example protocol
- ◆ Attack against the example protocol
- ◆ Formalizing secrecy by non-interference
- ◆ Proving secrecy by hedged bisimulations
- ◆ Conclusions



# Formalizing secrecy by non-interference

- ◆ "Definition": Process  $P$  keeps message  $x$  totally secret if  $[M/x]P$  and  $[N/x]P$  are "equivalent" for any  $M$  and  $N$

Cf. partial secrecy:  $[M/x]P$  and  $[N/x]P$  are equivalent for any  $M$  and  $N$  satisfying some condition (e.g.,  $M \bmod 2 = N \bmod 2$ )

- ◆ What equivalence should we take?  
⇒ (Strong) barbed equivalence

# Definitions (1/2)

- ◆ Process  $P$  immediately exhibits input barb  $c$ , written  $P \downarrow c$ , if

$$P \equiv (\nu x_1) \dots (\nu x_n) (c(y).Q \mid R)$$

for some  $x_1, \dots, x_n$  (distinct from  $c$ ),  $y$ ,  $Q$  and  $R$ .  
Similar for output.

- ◆ A (strong) barbed simulation  $S$  is a binary relation on processes such that  $P S Q$  implies:
  - for each barb  $\beta$ , if  $P \downarrow \beta$ , then  $Q \downarrow \beta$ , and
  - if  $P \rightarrow P'$ , then  $Q \rightarrow Q'$  and  $P' S Q'$  for some  $Q'$
- ◆  $S$  is a barbed bisimulation if both  $S$  and  $S^{-1}$  are barbed simulations

## Definitions (2/2)

- ◆ Barbed bisimilarity is the largest barbed bisimulation
  - Equals the union of all barbed bisimulations, which is also a barbed bisimulation
- ◆ Processes  $P$  and  $Q$  are barbed equivalent if  $P \mid R$  and  $Q \mid R$  are barbed bisimilar for every  $R$



# Example

- ◆  $(\nu k)\bar{c}\langle\{x\}_k\rangle$  keeps  $x$  totally secret.  
I.e.,  $(\nu k)\bar{c}\langle\{M\}_k\rangle$  and  $(\nu k)\bar{c}\langle\{N\}_k\rangle$  are barbed equivalent for any  $M$  and  $N$ .

Proof sketch: given  $M$  and  $N$ , take

$$S = \{ (P, Q) \mid \begin{array}{l} P \equiv (\nu k) [\{M\}_k/y]R, \\ Q \equiv (\nu k) [\{N\}_k/y]R, \\ k \notin \text{free}(R) \end{array} \}$$

and prove it to be a barbed bisimulation by case analysis (and induction) on the reduction rules



## Example

- ◆  $P = (\nu k)(\bar{c}\langle\{x\}_k\rangle \mid c(y).case\ y\ of\ \{z\}_k\ in\ \bar{c}\langle k\rangle)$  does not keep  $x$  totally secret. Indeed,  $[M/x]P$  and  $[N/x]P$  are not barbed equivalent for any  $M \neq N$ .

Proof: given  $M$  and  $N$ , take

$$R = c(y).\bar{c}\langle y\rangle.c(k).case\ y\ of\ \{m\}_k\ in\ [m = M]\overline{world}\langle hello\rangle$$

Cf.  $P = (\nu k)(\bar{k}\langle x\rangle \mid k(y).\bar{c}\langle k\rangle)$  does keep  $x$  secret



# Side Step: The Vice of May Testing Equivalence

- ◆ Many papers (including Abadi and Gordon's original work!) use may testing equivalence for defining secrecy by non-interference, but it is too weak



# Definitions

- ◆ Process  $P$  may eventually exhibit barb  $\beta$ , written  $P \Downarrow \beta$ , if  $P \rightarrow \dots \rightarrow P' \downarrow \beta$  for some  $P'$
- ◆ Processes  $P$  and  $Q$  are may testing equivalent if
$$(P \mid R) \Downarrow \beta \iff (Q \mid R) \Downarrow \beta$$
for every  $R$  and  $\beta$



# So what's wrong?

- ◆ Surprisingly,

$$P = (\nu d)(\bar{d}\langle \rangle \mid d().\bar{c}\langle \rangle)$$

and

$$Q = (\nu d)(\bar{d}\langle \rangle \mid d().\bar{c}\langle \rangle \mid d().0)$$

are may testing equivalent.

- ◆ As a result, processes like

**if  $x > 0$  then  $P$  else  $Q$**

are regarded as keeping  $x$  totally secret  
(under may testing equivalence)

- ◆ But the leak is possible!





# Outline

- ◆ What is spi-calculus?
  - Syntax and operational semantics
- ◆ Example protocol
- ◆ Attack against the example protocol
- ◆ Formalizing secrecy by non-interference
- ◆ Proving secrecy by hedged bisimulations
- ◆ Conclusions



# Hedged Bisimulation: Motivation

Direct proof of barbed equivalence is difficult because of "arbitrary R"

⇒ Devise a proof technique without "arbitrary R"

- ◆ What can R do?
  - Gain "knowledge" by receiving from a known channel
  - Send to a known channel a message synthesized from the knowledge

# Definitions (1/4)

- ◆ A hedge  $\mathcal{H}$  is a binary relation on messages
- ◆  $\mathcal{H} \vdash M \leftrightarrow N$  (messages  $M$  and  $N$  can be synthesized from hedge  $\mathcal{H}$ ) is defined by induction:

$$\frac{(M, N) \in \mathcal{H}}{\mathcal{H} \vdash M \leftrightarrow N} \quad \frac{\mathcal{H} \vdash M_1 \leftrightarrow N_1 \quad \mathcal{H} \vdash M_2 \leftrightarrow N_2}{\mathcal{H} \vdash \{M_1\}_{M_2} \leftrightarrow \{N_1\}_{N_2}}$$

$$\frac{\mathcal{H} \vdash \{M_1\}_{M_2} \leftrightarrow \{N_1\}_{N_2} \quad \mathcal{H} \vdash M_2 \leftrightarrow N_2}{\mathcal{H} \vdash M_1 \leftrightarrow N_1} \quad \frac{x \notin \text{free}(\mathcal{H})}{\mathcal{H} \vdash x \leftrightarrow x}$$

## Definitions (2/4)

- ◆ A hedged simulation is a set  $X$  of triples  $(P, Q, \mathcal{H})$  that satisfies:

1. For any  $P \rightarrow P'$ , there exists some  $Q'$  such that  $Q \rightarrow Q'$  and  $(P', Q', \mathcal{H}) \in X$ .

2. If for some  $\mathcal{H} \vdash c \leftrightarrow d$ ,

$$P \equiv (\nu x_1) \dots (\nu x_m) (\bar{c}\langle M \rangle.P_1 \mid P_2)$$

$$x_i \notin \{c\} \cup \text{free}(\text{fst}(\mathcal{H})),$$

$$\text{then } Q \equiv (\nu y_1) \dots (\nu y_n) (\bar{d}\langle N \rangle.Q_1 \mid Q_2)$$

$$y_i \notin \{d\} \cup \text{free}(\text{snd}(\mathcal{H}))$$

and  $(P_1 \mid P_2, Q_1 \mid Q_2, \mathcal{H} \cup (M, N)) \in X$ .

## Definitions (3/4)

3. If for some  $\mathcal{H} \vdash c \leftrightarrow d$ ,

$$P \equiv (\nu x_1) \dots (\nu x_m)(c(z).P_1 \mid P_2)$$

$$x_i \notin \{c\} \cup \text{free}(\text{fst}(\mathcal{H})),$$

then  $Q \equiv (\nu y_1) \dots (\nu y_n)(d(z).Q_1 \mid Q_2)$

$$y_i \notin \{d\} \cup \text{free}(\text{snd}(\mathcal{H}))$$

and for any  $\mathcal{H} \vdash M \leftrightarrow N$ ,

$$([M/z]P_1 \mid P_2, [N/z]Q_1 \mid Q_2, \mathcal{H}) \in X.$$

4. If  $\mathcal{H} \vdash M_1 \leftrightarrow N_1$  and  $\mathcal{H} \vdash M_2 \leftrightarrow N_2$ ,

then  $M_1 = M_2$  implies  $N_1 = N_2$ .

5. If  $\mathcal{H} \vdash \{M_1\}_{M_2} \leftrightarrow N$  and  $\mathcal{H} \vdash M_2 \leftrightarrow N_2$ ,

then  $N = \{N_1\}_{N_2}$  for some  $N_1$ .



## Definitions (4/4)

- ◆ A hedged simulation  $X$  is a hedged bisimulation if  $X^{-1}$  is also a hedged simulation, where  $X^{-1}$  is defined as:

$$\{(Q, P, H^{-1}) \mid (P, Q, H) \in X\}$$

- ◆ Hedged bisimilarity is the largest hedged bisimulation (i.e., the union of all hedged bisimulations, which is also a hedged bisimulation)
- ◆ Notation:  $P \sim_H Q \Leftrightarrow (P, Q, H)$  is in the hedged bisimilarity

# Caution: $\alpha$ -Conversion of Hedged Bisimulation

- ◆ Every  $(P, Q, H) \in X$  is regarded as  $\alpha$ -equivalent to
 
$$(\sigma P, Q, \{ (\sigma M, N) \mid (M, N) \in H \})$$
 for every  $\text{dom}(\sigma) \supseteq \text{free}(P) \cup \text{free}(\text{fst}(H))$
- ◆ Every  $(P, Q, H) \in X$  is regarded as  $\alpha$ -equivalent to
 
$$(P, \sigma Q, \{ (M, \sigma N) \mid (M, N) \in H \})$$
 for every  $\text{dom}(\sigma) \supseteq \text{free}(Q) \cup \text{free}(\text{snd}(H))$
- ◆ Everything in the rest is considered "up to" this  $\alpha$ -equivalence



# Example 1

- ◆ For any  $M$  and  $N$ ,

$$(\nu k)\bar{c}\langle\{M\}_k\rangle.0 \sim_{\{(c,c)\}} (\nu k)\bar{c}\langle\{N\}_k\rangle.0$$

Proof: take

$$\begin{aligned} X = & \{((\nu k)\bar{c}\langle\{M\}_k\rangle.0, \\ & (\nu k)\bar{c}\langle\{N\}_k\rangle.0, \\ & \{(c, c)\})\} \\ \cup & \{(0, \\ & 0, \\ & \{(c, c), (\{M\}_k, \{N\}_k)\})\} \end{aligned}$$

and check conditions 1-5.

## Example 2

- ◆  $(\nu k)(\nu n)\bar{c}\langle\{n\}_k\rangle.(\nu m)\bar{c}\langle m\rangle \sim \{(c,c)\}$   
 $(\nu k)(\nu n)\bar{c}\langle\{n\}_k\rangle.\bar{c}\langle n\rangle$

Proof: take

$$\begin{aligned}
 X &= \{((\nu k)(\nu n)\bar{c}\langle\{n\}_k\rangle.(\nu m)\bar{c}\langle m\rangle, \\
 &\quad (\nu k)(\nu n)\bar{c}\langle\{n\}_k\rangle.\bar{c}\langle n\rangle, \\
 &\quad \{(c,c)\})\} \\
 &\cup \{((\nu m)\bar{c}\langle m\rangle, \\
 &\quad \bar{c}\langle n\rangle, \\
 &\quad \{(c,c), (\{n\}_k, \{n\}_k)\})\} \\
 &\cup \{(0, \\
 &\quad 0, \\
 &\quad \{(c,c), (\{n\}_k, \{n\}_k), (m,n)\})\}.
 \end{aligned}$$

## Example 3

- ◆  $(\nu k)(\nu n)(\nu l)\bar{c}\langle\{\{n\}_k\}_l\rangle.(\nu m)\bar{c}\langle m\rangle \sim \{(c,c)\}$   
 $(\nu k)(\nu n)\bar{c}\langle\{n\}_k\rangle.(\nu m)\bar{c}\langle m\rangle$

Proof: take

$$\begin{aligned}
 X &= \{((\nu k)(\nu n)(\nu l)\bar{c}\langle\{\{n\}_k\}_l\rangle.(\nu m)\bar{c}\langle m\rangle, \\
 &\quad (\nu k)(\nu n)\bar{c}\langle\{n\}_k\rangle.(\nu m)\bar{c}\langle m\rangle, \\
 &\quad \{(c,c)\})\} \\
 &\cup \{((\nu m)\bar{c}\langle m\rangle, \\
 &\quad (\nu m)\bar{c}\langle m\rangle, \\
 &\quad \{(c,c), (\{\{n\}_k\}_l, \{n\}_k)\})\} \\
 &\cup \{(0, \\
 &\quad 0, \\
 &\quad \{(c,c), (\{\{n\}_k\}_l, \{n\}_k), (m,m)\})\}.
 \end{aligned}$$

# Theorem

Hedged bisimilarity is sound w.r.t. barbed equivalence. I.e., if  $P \sim_H Q$  for

$$H = \{ (x, x) \mid x \in \text{free}(P) \cup \text{free}(Q) \},$$

then  $P$  and  $Q$  are barbed equivalent.

Proof sketch: take

$$S = \{ (P', Q') \mid P \sim_H Q,$$

$$P' \equiv (\nu x_1) \dots (\nu x_l) (P \mid [M_1, \dots, M_n / z_1, \dots, z_n] R),$$

$$Q' \equiv (\nu y_1) \dots (\nu y_m) (Q \mid [N_1, \dots, N_n / z_1, \dots, z_n] R),$$

$$H \vdash M_1 \leftrightarrow N_1, \dots, H \vdash M_n \leftrightarrow N_n,$$

$$\text{free}(R) \text{ distinct from } \text{free}(P), \text{free}(Q), \text{ and } \text{free}(H) \}$$

and prove it to be a barbed bisimulation by case analysis (and induction) on the reduction rules.

# Real Example: Fixed Version of Previous Protocol

1.  $A \rightarrow S : \{K_{AB}, B\}_{K_{AS}}$   
 2.  $S \rightarrow B : \{K_{AB}, A\}_{K_{BS}}$   
 3.  $B \rightarrow A : \{M\}_{K_{AB}}$

1'.  $B \rightarrow S : \{K_{BE}, E\}_{K_{BS}}$   
 2'.  $S \rightarrow E : \{K_{BE}, B\}_{K_{ES}}$   
 3'.  $E \rightarrow B : \{M'\}_{K_{BE}}$

# As Spi-Calculus Processes...

$$\begin{aligned}
 P_A &= (\nu K_{AB}) \overline{c_{AS}} \langle \{K_{AB}, B\}_{K_{AS}} \rangle. \\
 &\quad c_{AB}(n). \text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0 \\
 P_S &= c_{AS}(x). \text{case } x \text{ of } \{y, b\}_{K_{AS}} \text{ in} \\
 &\quad [b = B] \overline{c_{BS}} \langle \{y\}_{K_{BS}} \rangle \\
 &\quad | c'_{BS}(x'). \text{case } x' \text{ of } \{y', e\}_{K_{BS}} \text{ in} \\
 &\quad [e = E] \overline{c_{ES}} \langle \{y'\}_{K_{ES}} \rangle \\
 P_B &= c_{BS}(x). \text{case } x \text{ of } \{y, a\}_{K_{BS}} \text{ in} \\
 &\quad [a = A] \overline{c_{AB}} \langle \{z\}_y \rangle \\
 &\quad | (\nu K_{BE}) c'_{BS} \langle \{K_{BE}, E\}_{K_{BS}} \rangle. \\
 &\quad c_{BE}(n'). \text{case } n' \text{ of } \{m'\}_{K_{BE}} \text{ in } 0
 \end{aligned}$$





## Exercise (?)

- ◆ Write down the reduction(s) of  $P'_E \mid (\nu K_{AS})(\nu K_{BS})(P_A \mid P_S \mid P_B)$  for the same attacker  $P'_E$  as before, for the fixed version of  $P_A$ ,  $P_S$ , and  $P_B$ . Pinpoint where the attack fails.

# Claim

- ◆  $(vK_{AS})(vK_{BS})(P_A | P_S | P_B)$   
keeps  $z$  totally secret. I.e.,

$$P = (vK_{AS})(vK_{BS})(P_A | P_S | [M/z]P_B)$$

and

$$Q = (vK_{AS})(vK_{BS})(P_A | P_S | [N/z]P_B)$$

are barbed equivalent for any  $M$  and  $N$ .



# Proof Sketch

- ◆ Let  $H = \{ (x, x) \mid x \in \text{free}(P) \cup \text{free}(Q) \}$
- ◆ We construct some hedged bisimulation  $X \ni (P, Q, H)$ 
  - The  $X$  is far from minimal, but this is fine as far as  $X$  is a hedged bisimulation
    - It is a nightmare to write down minimal  $X$  for real...



$$P_A = (\nu K_{AB}) \overline{c_{AS}} \langle \{K_{AB}, B\}_{K_{AS}} \rangle \cdot c_{AB}(n) \cdot \overbrace{\text{case } n \text{ of } \{m\}_{K_{AB}} \text{ in } 0}^{P_{A_2}}$$

$\overbrace{\hspace{15em}}^{P_{A_1}}$   
 $\overbrace{\hspace{25em}}^{P_{A_0}}$


$$P_S = c_{AS}(x) \cdot \text{case } x \text{ of } \{y, b\}_{K_{AS}} \text{ in } [b = B] \overline{c_{BS}} \langle \{y\}_{K_{BS}} \rangle$$

$\overbrace{\hspace{15em}}^{P_{S_3}}$   
 $\overbrace{\hspace{25em}}^{P_{S_1}}$   
 $\overbrace{\hspace{25em}}^{P_{S_0}}$

$$| c'_{BS}(x') \cdot \text{case } x' \text{ of } \{y', e\}_{K_{BS}} \text{ in } [e = E] \overline{c_{ES}} \langle \{y'\}_{K_{ES}} \rangle$$

$\overbrace{\hspace{15em}}^{P'_{S_3}}$   
 $\overbrace{\hspace{25em}}^{P'_{S_2}}$   
 $\overbrace{\hspace{25em}}^{P'_{S_1}}$   
 $\overbrace{\hspace{25em}}^{P'_{S_0}}$

$$\begin{array}{l}
 \overbrace{\hspace{10em}}^{P_{B_0}} \\
 \underbrace{\hspace{10em}}_{P_{B_1}} \\
 \underbrace{\hspace{10em}}_{P_{B_2}} \\
 \underbrace{\hspace{10em}}_{P_{B_3}} \\
 P_B = c_{BS}(x). \text{ case } x \text{ of } \{y, a\}_{K_{BS}} \text{ in } [a = A] \overline{c_{AB}}\langle\{z\}y\rangle \\
 | (\nu K_{BE}) \overline{c'_{BS}}\langle\{K_{BE}, E\}_{K_{BS}}\rangle. \underbrace{c_{BE}(n'). \text{ case } n' \text{ of } \{m'\}_{K_{BE}} \text{ in } 0}_{P'_{B_2}} \\
 \underbrace{\hspace{10em}}_{P'_{B_1}} \\
 \underbrace{\hspace{10em}}_{P'_{B_0}}
 \end{array}$$



$$\begin{aligned}
 X = \{ (P', Q', H') \mid \\
 P' \equiv & (vc_1) \dots (vc_u) \\
 & ([M_1/n]P_{A_i} \mid [M_2/x]P_{S_i} \mid [M_3, A/x', e]P'_{S_k} \mid \\
 & [M_4, E, M/x, a, z]P_{B_l} \mid [M_5/n']P'_{B_m}), \\
 Q' \equiv & (vd_1) \dots (vd_v) \\
 & ([N_1/n]P_{A_i} \mid [N_2/x]P_{S_i} \mid [N_3, A/x', e]P'_{S_k} \mid \\
 & [N_4, E, N/x, a, z]P_{B_l} \mid [N_5/n']P'_{B_m}), \\
 H' \subseteq & H \cup \{ (\{K_{AB}, B\}_{K_{AS}}, \{K_{AB}, B\}_{K_{AS}}), \\
 & (\{K_{AB}, A\}_{K_{BS}}, \{K_{AB}, A\}_{K_{BS}}), \\
 & (\{M\}_{K_{AB}}, \{N\}_{K_{AB}}), \\
 & (\{K_{BE}, E\}_{K_{BS}}, \{K_{BE}, E\}_{K_{BS}}), \\
 & (\{K_{BE}, B\}_{K_{ES}}, \{K_{BE}, B\}_{K_{ES}}) \}, \\
 H' \vdash & M_w \leftrightarrow N_w \text{ for } w = 1, 2, 3, 4, 5, \\
 c_1, \dots, c_u & \notin \text{free}(\text{fst}(H')), \\
 d_1, \dots, d_v & \notin \text{free}(\text{snd}(H')) \}
 \end{aligned}$$



## Exercise (?)

- ◆ Try to prove the total secrecy of  $z$  in the original version of this protocol by means of hedged bisimulation. Explain how the "proof" fails.

# Side Step II: Completeness of Hedged Bisimulation

Conjecture:

Hedged bisimilarity is complete with respect to barbed equivalence.

I.e., if  $P$  and  $Q$  are barbed equivalent, then  $P \sim_H Q$  for

$$H = \{ (x, x) \mid x \in \text{free}(P) \cup \text{free}(Q) \}$$

- Proved for "structurally image finite" processes, but not for the general case (to my knowledge)







# Outline

- ◆ What is spi-calculus?
  - Syntax and operational semantics
- ◆ Example protocol
- ◆ Attack against the example protocol
- ◆ Formalizing secrecy by non-interference
- ◆ Proving secrecy by hedged bisimulations
- ◆ Conclusions

# Other Topics in Spi-Calculus

- ◆ Other bisimulations [Abadi-Gordon 98]  
[Boreale-DeNicola-Pugliese 99]  
[Elkjær-Höhle-Hüttel-Overgård 99]
  - More complex and "less complete"
- ◆ Secrecy by typing [Abadi 97]  
[Abadi-Blanchet 01]
- ◆ Authenticity by typing [Gordon-Jeffery 01]  
[Gordon-Jeffery 02] [Blanchet 02]

Cf. <http://www.soe.ucsc.edu/~abadi/>  
<http://www.di.ens.fr/~blanchet/>  
<http://netlib.bell-labs.com/who/ajeffrey/> etc.

